

ORBITAL ELEMENTS, DYNAMICAL MASSES AND PARALLAXES FOR FOUR DOUBLE AND ONE TRIPLE SYSTEMS

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SUMMARY: New orbital elements for four binaries: WDS 00416+2438 = WRH 28, WDS 01554+0257 = A 2407 = ADS 1530, WDS 15031+4439 = CHR 43 and WDS 22550+5132 = HU 785 = ADS 16368 and one triple star WDS 23393+4543 = ADS 16904: CHR 149 Aa and A 643 Aa-B are determined. Preliminary dynamical masses and parallaxes are also given.

Key words. binaries: visual

1. INTRODUCTION

New orbital elements for three binaries WRH 28, A 2407, and CHR 43, and for a pair - A 643 Aa-B - belonging to the triple ADS 16904, calculated from observations which were at our disposal were published in the IAUDS Information Circular No. 154 (Olević and Cvetković 2004b). In the case of binary HU 785 and a pair CHR 149 Aa, belonging to the triple system ADS 16904, some missing observational results were kindly provided by Prof. J. Docobo so, that we could calculate their new orbital elements and publish them in the IAUDS Information Circular No. 155 (Olević and Cvetković 2005). Here we give a complete analysis of the obtained results - orbital elements, calculated dynamical masses of the components, i.e. the total mass of the system, and the dynamical parallaxes for the three systems.

Pair WRH 28 was discovered by R.H. Wilson in 1949, but he could not measure the coordinates due to the small separation between the components. From the date of discovery till 1988, there were five successful measurements for this pair, all of them by means of the speckle interferometry. The orbital elements were first calculated from four measurements (Olević and Jovanović 1999). The orbit was also published in the Fifth Catalog of Orbits of Visual Binary

Stars (Hartkopf et al. 2001). The obtained values were 3.151 years for the period, $0''.285$ for the semi-major axis. The total mass of the system following from these values and the Hipparcos trigonometric parallax π_{HIP} (about $30M_{\odot}$) for the given spectral type A7m is too large.

For binary A 2407, the orbital elements were first determined by Baize (1984).

In the case of HU 785, the first to determine the orbital elements was Zulević (1980).

For the triple system ADS 16904 = A 643 Aa-B and ADS 16904 = CHR 149 Aa, the orbital elements were calculated by Balega and they were published in the Sixth Catalog of Orbits of Visual Binary Stars (Hartkopf and Mason 2003).

For these five pairs, recent observations indicate significant deviations from the orbits obtained by the authors mentioned above. Therefore it is necessary to redetermine the orbital elements for these binaries.

For the binary CHR 43, from its discovery in 1985 till 1995, a total of ten measurements is available; all of them were done by means of the speckle interferometry. The observations cover an arc of 119 degrees. For this system no one before us calculated the orbital elements, hence those published in the IAUDS Information Circular No. 154 define the first orbit ever calculated for this pair.

2. THE METHOD, RESULTS AND DISCUSSION

2.1. Method

In the calculations of orbital elements we used the KOVOLE method, developed by one of us (D. Olević; see Olević and Cvetković 2004a). This method is based on Kovalski's method and yields satisfactory results from interferometric measurements even when only a short orbital arc is covered by the observations. The original method has failed in this situation. A correct estimate of the observational weights is of particular importance. For this purpose we use a criterion analogous to that applied by Mason et al. (1999). Individual masses and dynamical parallaxes are calculated using Angelov's (1993) relation.

2.2. Results

The orbital elements (equinox J2000) and the corresponding errors are listed in Table 1: m_A and m_B are the apparent magnitudes of the components taken from the WDS Catalog (Mason et al. 2003); v denotes the total magnitude. The spectral type is also taken from WDS.

Table 2 contains the observational data and their residuals ($\Delta\theta^\circ$ and $\Delta\rho''$). Asterisks (*) mark observations subject to a change of quadrant. Double asterisks (**) indicate the measurements not used in the orbit calculation. The sign (\diamond) indicates the interferometric measurements. The corresponding ephemeris values are given in the parentheses.

The ephemerides for 2005-2009 are given in Table 3.

In Figs. 1-6 we give the fitted orbits and the lines of nodes. The visual observations are presented by filled circles and those observed interferometrically by filled squares. The empty circles and empty squares are their corresponding ephemeris positions. The dashed line gives the rejected observations. The arrow indicates the sense of the orbital motion.

Comments

WDS 00416+2438 = WRH 28: By adding the last measurement from 1988.898 unavailable to us in the previous determination of orbital elements (Olević and Jovanović 1999), we found that the measurement from 1983.9307 possessed a large error. Namely, after calculating the orbital elements without it, the values obtained for the period and semimajor axis were: $P=21.262$ years, $a=0''.126$, respectively. Using the Hipparcos trigonometric parallax, $\pi_{\text{HIP}} = 0''.00706 \pm 0''.00077$, one obtains $12.6M_\odot$ for the total mass of the system, which can be expected for the spectral type A7m. Due to the small number of measurements, the results can be considered as preliminary. Since this pair has an interesting spectral type and its calculated period is relatively short, we would recommend it to be observed more frequently.

WDS 01554+0257 = A 2407: The individual component masses ($1.0M_\odot$ and $0.8M_\odot$) are within those expected for their spectral type K0. The calculated dynamical parallax $\pi_{\text{dyn}} = 0''.018$

agrees well with the Hipparcos trigonometric parallax $\pi_{\text{HIP}} = 0''.02317 \pm 0.00302$, considering the error limits including the uncertainties for P and a , as well. This pair also deserves to be measured more frequently since the orbit part already passed by it is about 50%; consequently one can expect a significantly more reliable determination of orbital elements soon.

WDS 15031+4439 = CHR 43: This relatively very bright pair was discovered by means of the speckle interferometry in 1985. It was named after CHARA (Center for High Angular Resolution Astronomy) Programme of the Georgia State University, Atlanta, USA. The fact that it belongs to Luminosity Class IV (HR - F6IV) makes this system interesting. The Hipparcos trigonometric parallax leads to a total mass of $1.6M_\odot$. The measurements of the position angle bear significant errors. This is due to the impossibility of resolving the components visually.

WDS 22550+5132 = HU 785: This faint pair was discovered by Hussey in 1902. However, until 1991 it had been measured 11 times only. The last measurement was made by the Hipparcos Satellite. All the measurements (except the last one) were classical micrometric ones. The pair passed an arc of 124 degrees. Heinz's measurement in 1976 had a large error in the position angle and, it is not used in the calculation of the orbital elements. The obtained individual component masses $1.4M_\odot$ and $1.3M_\odot$ are in a good agreement with what can be expected for the spectral type F2. The calculated dynamical parallax $\pi_{\text{dyn}} = 0''.0049$ is in agreement with the Hipparcos trigonometric parallax $\pi_{\text{HIP}} = 0''.00318 \pm 0.00129$ within the error limits when the uncertainties of all parameters are taken into account.

WDS 23393+4543: This system was discovered by Aitken in 1903 as double and given A 643 as its designation. That its A component is also double, i.e. the system as a whole is triple, became known in 1986 in the framework of the CHARA programme. Since that time, the designation for the system discovered first has been **A 643 Aa-B**, whereas the subsystem has been referred to as **CHR 149 Aa**. The first orbital elements for both A 643 Aa-B and CHR 149 Aa were calculated in 1999 by Balega. According to our calculations, the period P for pair A 643 Aa-B is 2.14 times longer than that obtained by Balega; similarly, the period for pair CHR 149 Aa amounts to 0.30 times that obtained by Balega. The dynamical masses of the components for A 643 Aa-B are found to be $2.2M_\odot$, both being in agreement with the expectations based on the spectral type A2. The calculated dynamical parallax $\pi_{\text{dyn}} = 0''.0033$ nearly coincides with the Hipparcos trigonometric parallax $\pi_{\text{HIP}} = 0''.00370 \pm 0.00127$. Large residuals of the recent measurements from the orbit fitted on the basis of Balega's elements (e.g. in case of CHR 149 Aa for epoch 1999.821 the residuals are $+126^\circ.5$ and $-0''.017$, whereas in case of pair A 643 Aa-B the residuals for epoch 1999.7282 are $+5^\circ.6$ and $+0''.041$) are in favour of our results.

The orbits of all the three components are in the same plane (inclination for both pairs is $i = 147$ degrees) which confirms one of the hypotheses on the formation of multiple stars.

Table 1. Orbital elements

Name	WRH 28	A 2407	CHR 43	HU 785	CHR 149 Aa	A 643 Aa-B
WDS	00416+2438	01554+0257	15031+4439	22550+5132	23393+4543	23393+4543
HIP	3269	8958	73637	113166	116726	116726
m_A, m_B	$v = 6.0$	10.05-10.50	$v = 6.65$	9.91-10.36	$v = 7.63$	8.45-8.49
Sp	A7m	K0	F6IV	F2	A2	A2
P (yr)	21.26±0.94	183.87±4.40	97.70±4.82	266.82±15.00	20.28±0.40	324.38±6.28
T	1993.02±0.56	1971.43±4.14	2078.87±0.45	2125.41±5.32	1999.65±0.24	1926.27±7.12
a ($''$)	0.126±0.006	0.689±0.061	0.430±0.056	0.285±0.020	0.040±0.002	0.261±0.003
e	0.50±0.04	0.07±0.03	0.52±0.11	0.27±0.04	0.23±0.04	0.11±0.01
i ($^\circ$)	33.4±3.6	46.0±2.9	71.8±2.4	109.8±1.4	147.1±4.5	147.5±1.4
Ω ($^\circ$)	145.7±6.7	172.8±4.8	62.8±3.0	87.7±2.5	58.7±9.2	30.5±2.9
ω ($^\circ$)	230.5±8.0	45.3±25.6	358.0±3.8	108.6±14.2	219.2±12.3	152.6±5.4
$\mathcal{M}_A(\odot)$	—	1.0	—	1.4	—	2.2
$\mathcal{M}_B(\odot)$	—	0.8	—	1.3	—	2.2
$\Sigma\mathcal{M}$	12.6 ± 4.9	—	1.6 ± 1.0	—	3.0 ± 3.3	—
π_{dyn} (mas)	—	18	—	5	—	3
π_{HIP} (mas)	7.06 ± 0.77	23.17 ± 3.02	17.45 ± 0.67	3.18 ± 1.29	3.70 ± 1.27	3.70 ± 1.27

Table 2. Observations and residuals

WDS 00416+2438 = WRH 28

t	θ°	ρ''	n	Obs.	$\Delta\theta^\circ$	$\Delta\rho''$
1980.7232 $^\circ$	179.3	0.170	1	McA	-0.9	-0.004
1982.7601 $^\circ$	195.6	0.178	1	McA	2.1	0.008
1983.9307 $^\circ$ **	182.5	0.145	1	Bnu	(-19.3	-0.018)
1984.9991 $^\circ$	208.5	0.148	1	McA	-1.5	-0.007
1988.8982 $^\circ$	252.6	0.116	1	Hrt	0.3	0.002

WDS 01554+0257 = A 2407

t	θ°	ρ''	n	Obs.	$\Delta\theta^\circ$	$\Delta\rho''$
1912.74	103.9	0.53	3	A	2.5	0.021
1919.88	117.8	0.53	2	A	-0.6	-0.007
1939.73	158.8	0.56	1	VBS	3.4	-0.079
1940.676	159.7	0.55	1	VBS	2.8	-0.092
1941.906	159.0	0.62	1	VBs	0.2	-0.025
1948.786	160.3	0.74	1	VBS	-8.9	0.086
1951.420	171.2	0.63	1	VBS	-1.9	-0.022
1950.930	177.5	0.78	1	MRZ	5.1	0.127
1951.920	174.6	0.69	1	MRZ	0.7	0.039
1955.026	184.8	0.56	1	COU	6.1	-0.084
1958.060	178.3	0.54	4	VBS	-5.2	-0.094
1960.770	190.1	0.67	4	WOR	2.2	0.049
1961.758	189.7	0.55	3	WOR	0.1	-0.065
1963.850	191.9	0.74	2	VBS	-1.3	0.137
1974.970	207.3	0.61	3	HEI	-8.6	0.088
1978.810	226.5	0.44	3	HEI	1.0	-0.055
1981.860	235.6	0.42	3	HEI	1.9	-0.057
1984.996	250.4	0.44	4	WOR	7.5	-0.022
1991.250	267.0	0.472	1	HIP	4.6	0.019
1991.750	261.4	0.500	1	TYC	-2.6	0.047

Table 2. (continued)

WDS 15031+4439 = CHR 43

t	θ°	ρ''	n	Obs.	$\Delta\theta^\circ$	$\Delta\rho''$
1985.5171 $^\diamond$	84.4	0.169	1	McA	0.4	0.007
1986.4070 $^\diamond$	90.9	0.168	1	McA	-0.0	0.023
1988.1628 $^\diamond$	112.0	0.128	1	McA	1.5	0.014
1988.2527 $^\diamond$	104.9	0.115	1	McA	-6.8	0.002
1989.2274 $^\diamond$	116.8	0.083	1	McA	-10.5	-0.019
1991.3246 $^\diamond$	175.4	0.100	1	McA	10.3	-0.006
1991.3297 $^\diamond$	173.9	0.102	2	McA	8.8	-0.004
1992.3102 $^\diamond$	184.1	0.134	1	McA	4.8	0.014
1995.1498 $^\diamond$	200.1	0.191	1	Hrt	-3.3	0.010
1995.3109 $^\diamond$	203.6	0.180	1	Hrt	-0.7	-0.005

WDS 22550+5132 = HU 785

t	θ°	ρ''	n	Obs.	$\Delta\theta^\circ$	$\Delta\rho''$
1902.5300	261.5	0.250	1	HU	0.2	-0.002
1903.5800	260.2	0.250	2	HU	-0.5	-0.002
1922.7400	250.1	0.230	3	VBS	1.3	0.006
1946.4000	227.5	0.190	4	VBS	2.5	0.033
1954.7000	202.7	0.120	5	VBS	-8.3	-0.016
1957.0000	198.9	0.100	1	IDS	-7.5	-0.031
1976.8100**	63.7	0.170	2	HEI	(-96.1	0.043)
1980.7000	172.9	0.130	2	HEI	21.3	-0.004
1981.5900	157.4	0.120	3	HEI	7.5	-0.016
1988.8270	124.1	0.180	1	GIL	-13.4	0.026
1991.2500*	317.0	0.176	1	HIP	3.0	0.015

WDS 23393+4543 = CHR 149 Aa

t	θ°	ρ''	n	Obs.	$\Delta\theta^\circ$	$\Delta\rho''$
1986.8914 $^\diamond$	53.5	0.048	1	McA	2.1	0.001
1988.6578 $^\diamond$	31.0	0.048	1	McA	-2.3	0.001
1993.8413 $^\diamond$	323.6	0.040	1	Bag	-2.4	0.003
1994.7237 $^\diamond$ *	131.0	0.033	1	Sco	0.6	-0.002
1998.7745 $^\diamond$	223.1	0.029	1	Bag	-3.9	-0.002
1999.8210 $^\diamond$ *	26.2	0.028	1	Bag	6.8	0.000

Table 2. (continued)
WDS 23393+4543 = A 643 Aa-B

t	θ°	ρ''	n	Obs.	$\Delta\theta^\circ$	$\Delta\rho''$
1903.9300	264.3	0.210	1	A	-0.1	0.001
1911.6300	251.5	0.190	1	A	-1.9	-0.024
1916.9400	247.4	0.230	1	A	1.2	0.013
1921.5500	241.5	0.220	1	A	1.4	-0.001
1934.6700	223.9	0.240	1	A	0.3	0.011
1944.5700	208.3	0.220	1	VOU	-3.7	-0.014
1944.8300	219.8	0.230	1	VBS	8.1	-0.004
1953.7500	202.2	0.260	3	MUL	0.1	0.025
1956.8600	195.8	0.270	2	COU	-2.1	0.035
1959.0000	195.0	0.200	1	IDS	-0.4	-0.035
1959.8400*	11.0	0.270	1	COU	-3.4	0.035
1961.8100*	10.6	0.230	1	COU	-1.6	-0.005
1962.7800	190.8	0.240	1	HEI	-0.3	0.005
1964.8900	187.3	0.240	1	HIE	-1.3	0.005
1965.4900	181.7	0.220	2	COU	-6.2	-0.014
1966.2600	195.5	0.240	2	MUL	8.4	0.006
1971.8100	183.9	0.240	1	HEI	3.2	0.007
1973.2370*	2.0	0.260	1	WOR	3.1	0.027
1975.7626**	155.6	0.220	5	HAR	(-20.4	-0.012)
1976.7100	178.9	0.240	1	HEI	4.1	0.008
1983.7103 \diamond	165.7	0.235	1	McA	-0.8	0.006
1985.8373 \diamond	157.3	0.226	1	McA	-6.6	-0.003
1986.8914 \diamond	156.4	0.225	1	McA	-6.2	-0.004
1987.7540 \diamond	155.2	0.229	1	McA	-6.4	0.001
1988.6578 \diamond	156.3	0.218	1	McA	-4.2	-0.010
1989.7173 \diamond	158.1	0.210	1	Hrt	-1.1	-0.018
1989.7173	158.1	0.210	1	HEI	-1.0	-0.018
1991.2500	158.0	0.226	1	HIP	0.7	-0.001
1993.8413 \diamond	154.1	0.214	1	Bag	0.0	-0.013
1994.7237 \diamond *	335.5	0.212	1	Sco	2.5	-0.015
1994.9000	151.5	0.250	1	HEI	-1.3	0.023
1995.7626 \diamond	155.6	0.220	1	Hrt	3.9	-0.007
1996.5404 \diamond	154.2	0.226	1	Hrt	3.4	0.000
1998.7745 \diamond *	333.3	0.237	1	Bag	5.3	0.011
1999.7282 \diamond	150.2	0.239	1	Doc	3.4	0.013

Table 3. Ephemerides

t	A 2145		BU 368 AB		STF 2909 AB		A 2695		FIN 375 Aa		McA 76	
	θ°	ρ''	θ°	ρ''	θ°	ρ''	θ°	ρ''	θ°	ρ''	θ°	ρ''
2005.0	200.4	.164	301.2	.522	227.2	.405	119.1	.204	76.2	.042	140.3	.226
2006.0	207.9	.157	303.6	.530	228.3	.424	118.2	.208	64.1	.045	139.1	.226
2007.0	216.2	.149	305.8	.538	229.3	.442	117.4	.211	53.2	.047	137.8	.226
2008.0	225.7	.139	308.0	.547	230.2	.460	116.6	.214	42.9	.047	136.6	.226
2009.0	236.7	.128	310.2	.555	231.0	.476	115.8	.217	32.6	.047	135.3	.226

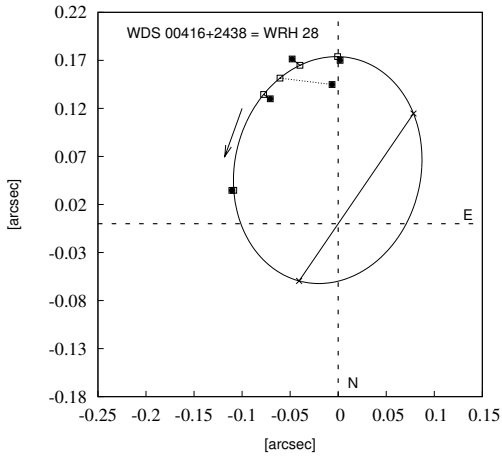


Fig. 1. *Orbit of WRH 28.*

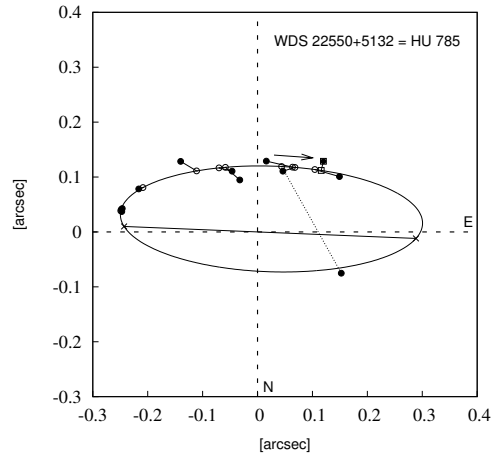


Fig. 4. *Orbit of HU 785.*

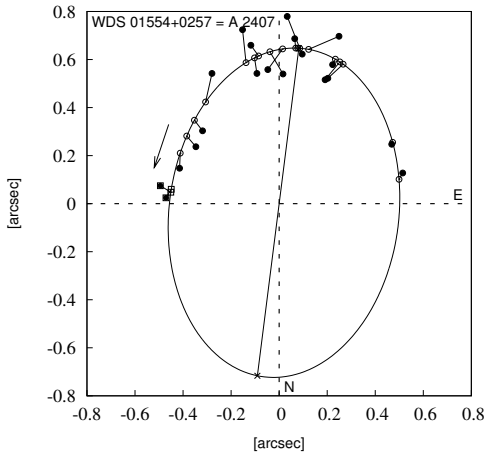


Fig. 2. *Orbit of A 2407.*

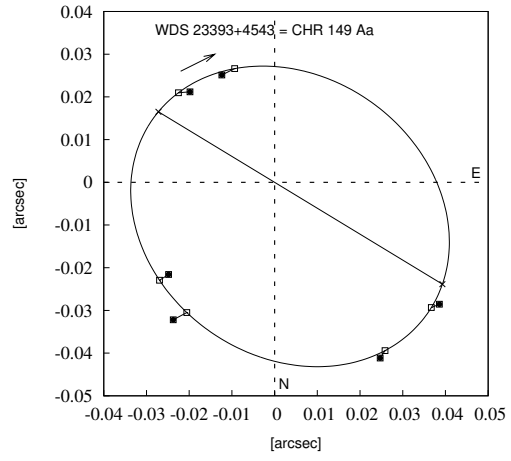


Fig. 5. *Orbit of CHR 149 Aa.*

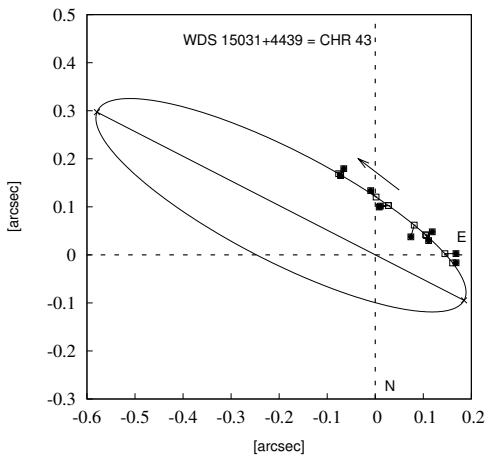


Fig. 3. *Orbit of CHR 43.*

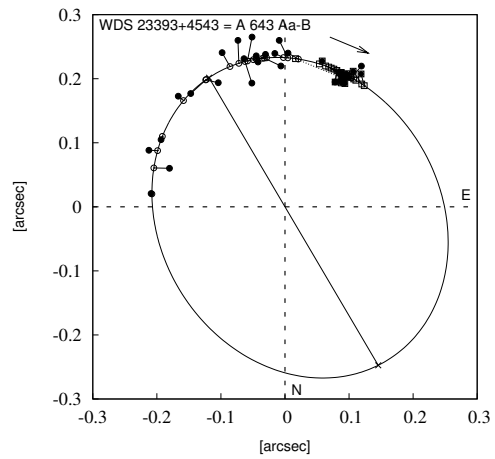


Fig. 6. *Orbit of A 643 Aa-B.*

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ОРБИТАЛНИ ЕЛЕМЕНТИ, ДИНАМИЧКЕ МАСЕ И ПАРАЛАКСЕ ЗА ЧЕТИРИ ДВОЈНА И ЈЕДАН ТРОЈНИ СИСТЕМ

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Оригинални научни рад

У раду су дати нови путањски елементи за четири двојна система: WDS 00416+2438 = WRH 28, WDS 01554+0257 = A 2407 = ADS 1530, WDS 15031+4439 = CHR 43 и WDS 22550+5132 = HU 785 = ADS 16368 и за тројни

систем WDS 23393+4543 = ADS 16904: CHR 149 Aa и A 643 Aa-B. Поред тога дате су и прелиминарне динамичке масе и динамичке паралаксе.